



# Security and Privacy in Wireless Networks

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Chapter 10: ([secowinet.epfl.ch](http://secowinet.epfl.ch))

Packet Forwarding in Ad Hoc Networks

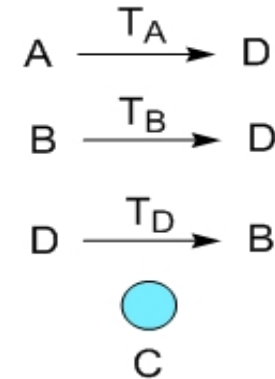
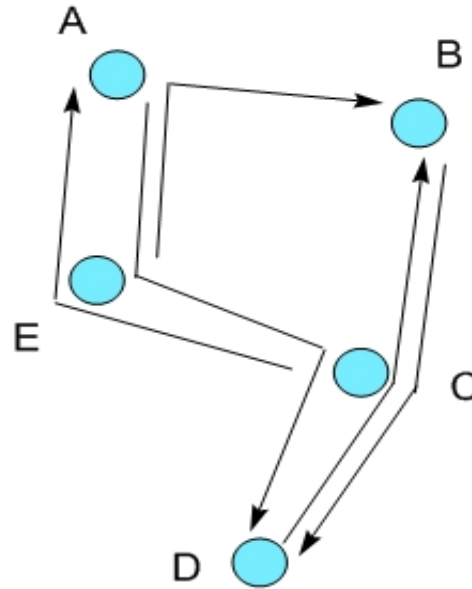
# **SELFISHNESS IN PACKET FORWARDING**

# Introduction

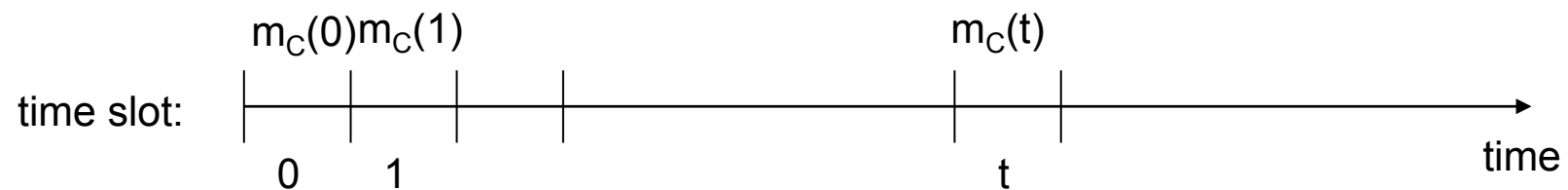
- The operation of multi-hop wireless networks requires the nodes to forward data packets on behalf of other nodes
- However, such cooperative behavior has no direct benefit for the forwarding node, and it consumes valuable resources (battery)
- Hence, the nodes may tend to behave selfishly and deny cooperation
- If many nodes defect, then the operation of the entire network is jeopardized
- **Questions:**
  - What are the conditions for the emergence of cooperation in packet forwarding?
  - Can it emerge spontaneously or should it be stimulated by some external mechanism?

# Modeling packet forwarding as a game

**Players:** nodes



**Strategy:**  
cooperation  
level



**Benefit** (of node  $i$ ):  
proportion of packets sent by node  $i$  reaching their destination

# Cost function

**Cost for forwarder  $f_j$ :**

$$c_{f_j}(r, t) = -T_s(r) \cdot C \cdot \hat{\tau}_j(r, t)$$

where:

$T_s(r)$  – traffic sent by source  $s$  on route  $r$   
 $C$  – unit cost of forwarding

**Example :**

$$\hat{\tau}_C(r, t) = \prod_{k \in \{E, C\}} m_{f_k}(t) = m_E(t) \cdot m_C(t)$$

$$c_C(r, t) = -T_A(r) \cdot C \cdot \hat{\tau}_j(r, t)$$

**Normalized throughput at forwarder  $f_j$ :**

$$\hat{\tau}_j(r, t) = \prod_{k=1}^j m_{f_k}(t)$$

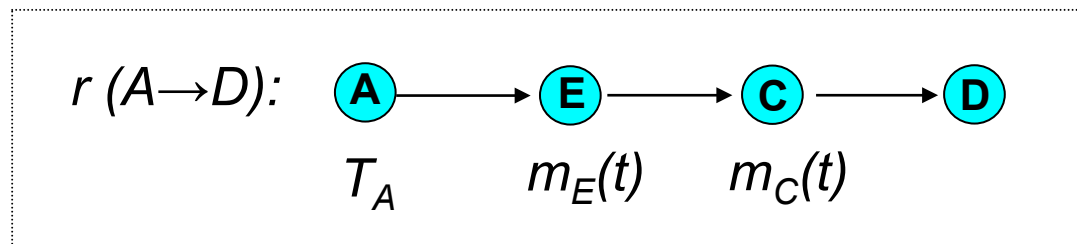
where:

$r$  – route on which  $f_k$  is a forwarder

$t$  – time slot

$f_k$  – forwarders on route  $r$

$m_{f_k}$  – cooperation level of forwarder  $f_k$



# Benefit function

**Experienced throughput :**

$$\tau(r, t) = T_s(r) \cdot \prod_{k=1}^l m_{f_k}(t)$$

where:  $s$  – source

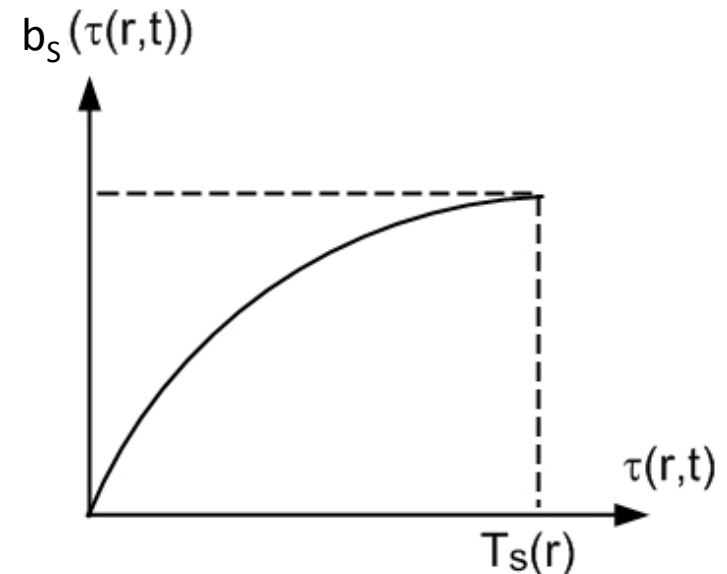
$r$  – route on which  $s$  is a source

$t$  – time slot

$f_k$  – forwarders for  $s$

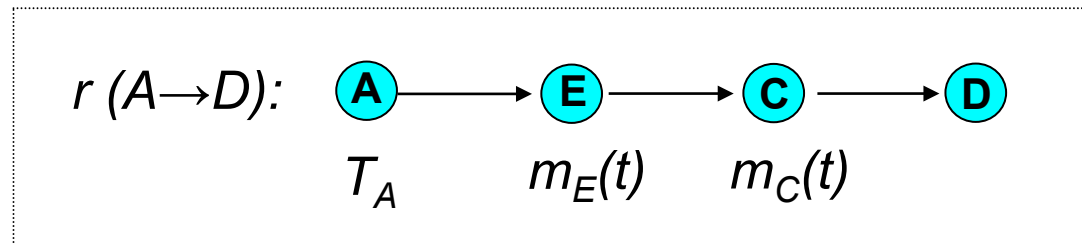
$p_{f_k}$  – cooperation level of forwarder  $f_k$

**benefit function :**



**Example :**

$$\tau(r, t) = T_A(r) \cdot m_E(t) \cdot m_C(t)$$



# Total payoff

**Payoff = Benefit - Cost**

$$u_i(t) = \sum_{q \in S_i(t)} b_i(\tau(q, t)) + \sum_{r \in F_i(t)} c_i(r, t)$$

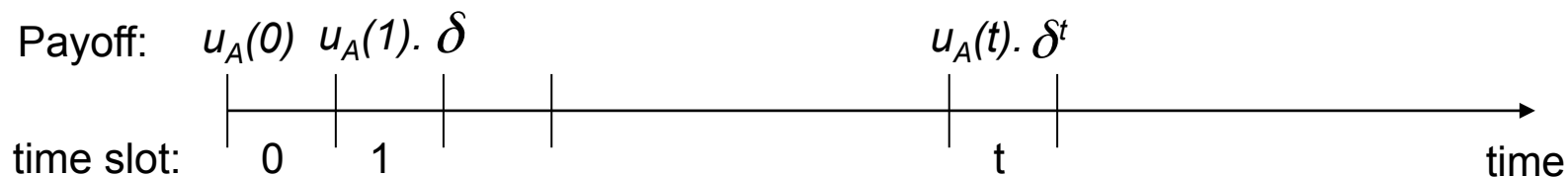
where:  $S_i(t)$  – set of routes on which  $i$  is a source  
 $F_i(t)$  – set of routes on which  $i$  is a forwarder

The goal of each node is to maximize its total payoff over the game:

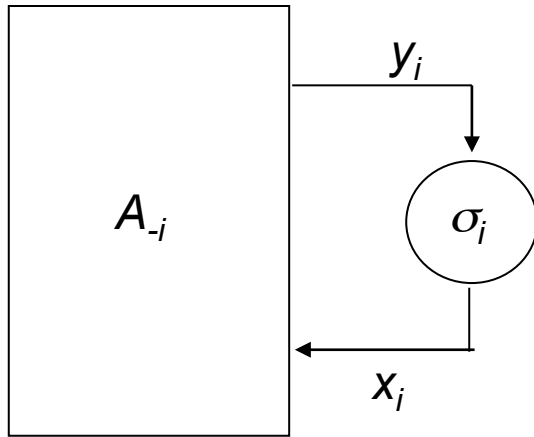
$$\sum_{t=0}^{\infty} u_i(t) \cdot \delta^t$$

where:  $\delta$  – discounting factor  
 $t$  – time

**Example :**



# Representation of the Nodes as Players



Strategy function for node  $i$ :

$$m_i(t) = \sigma_i([\tau(r, t - 1)])$$

where:

$\tau(r, t)$  – experienced throughput

Node  $i$  is playing against the rest of the network (represented by the box denoted by  $A_{-i}$ )



# Examples of Strategies

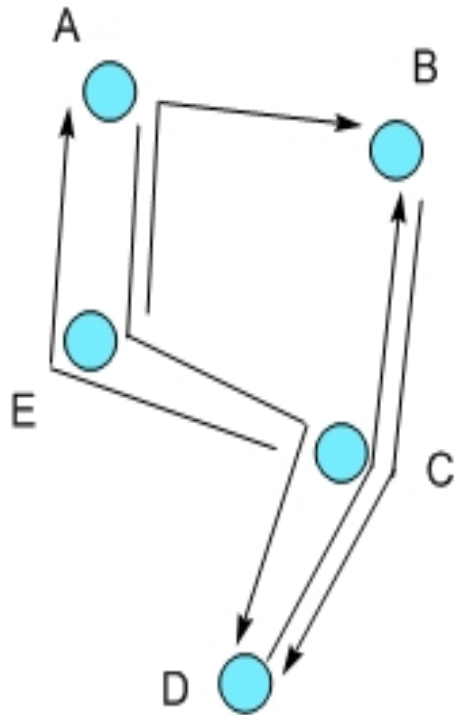
Strategy	Initial cooperation level	Function $\sigma_i(y_i) = x_i$
AlID (always defect)	0	$\sigma_i(y_i) = 0$
AlIC (always cooperate)	1	$\sigma_i(y_i) = 1$
TFT (Tit-For-Tat)	1	$\sigma_i(y_i) = y_i$

where  $y_i$  stands for the input

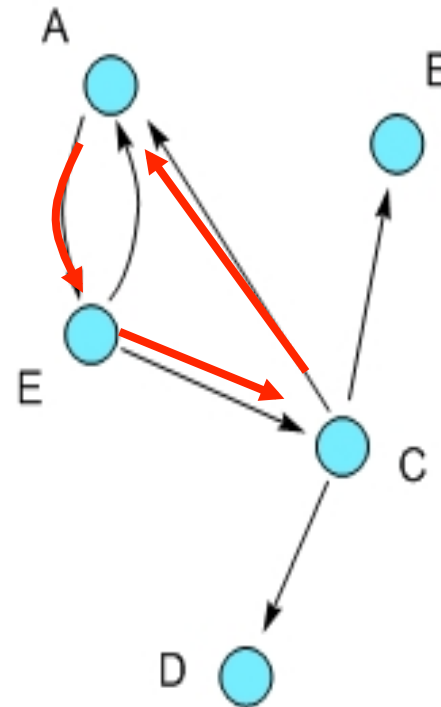
- **non-reactive strategies:**  
the output of the strategy function  
is independent of the input (example: AlID and AlIC)
- **reactive strategies:**  
the output of the strategy function  
depends on the input (example: TFT)

# Concept of Dependency Graph

**dependency:** the benefit of each source is dependent on the behavior of its forwarders



(a) routes

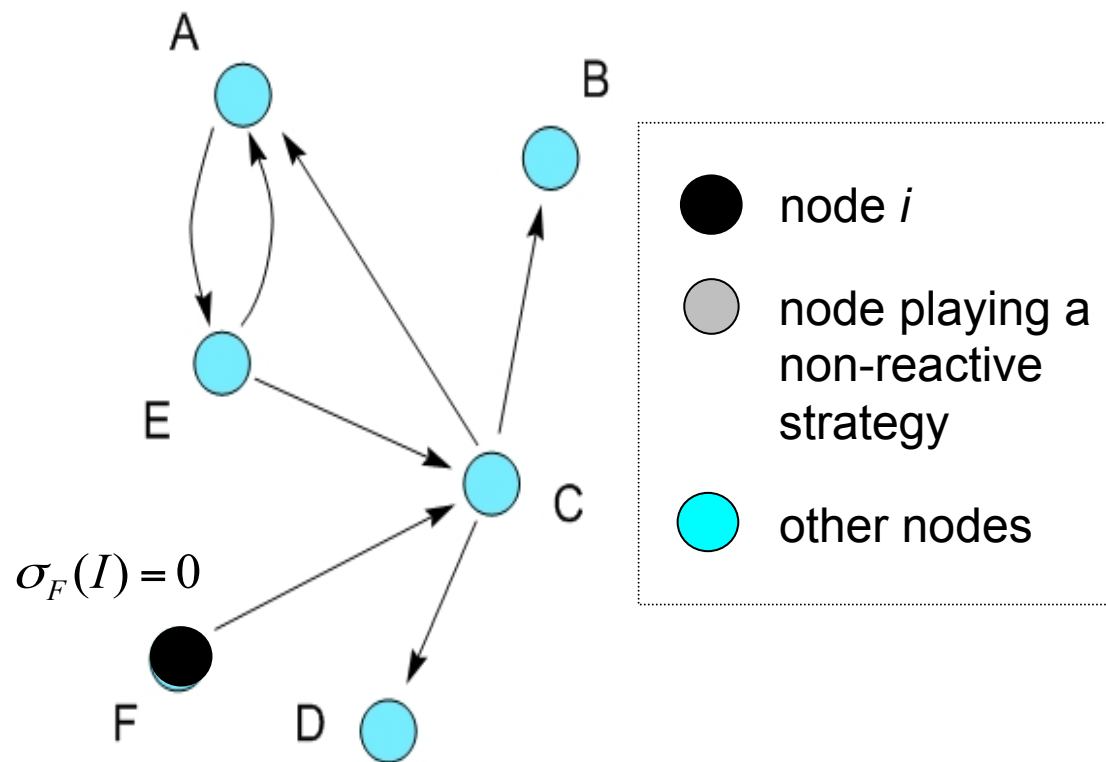


(b) dependency graph

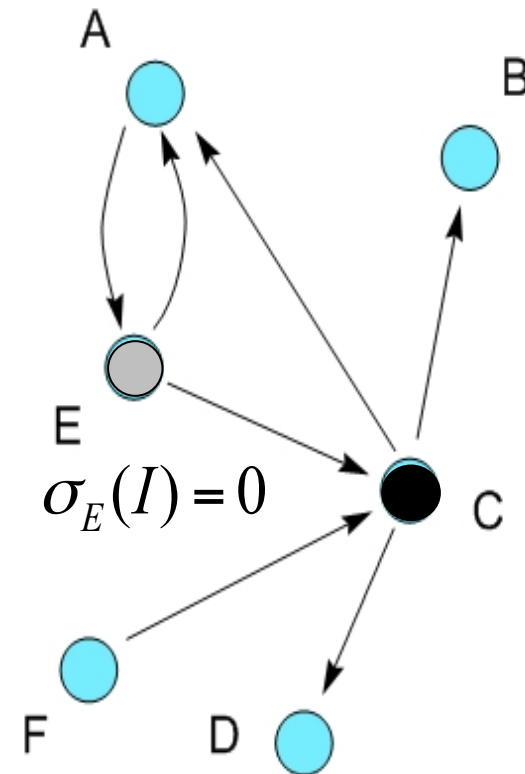
dependency  
loop

# Analytical Results (1/2)

**Theorem 1:** If node  $i$  does not have any dependency loops, then its best strategy is AllD.



**Theorem 2:** If node  $i$  has only non-reactive dependency loops, then its best strategy is AllD.



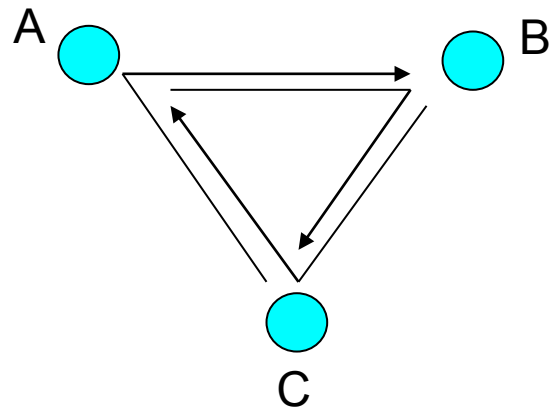
**Corollary 1:** If every node plays AllD, it is a Nash-equilibrium.

# Analytical results (2/2)

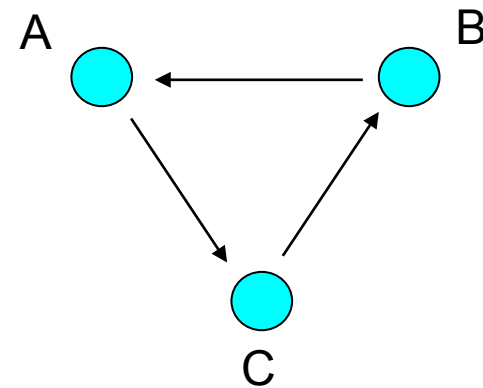
**Theorem 3 (simplified):** Assuming that node  $i$  is a forwarder, its behavior will be cooperative only if it has a dependency loop with each of its sources

**Corollary 2:** If Theorem 3 holds for every node, it is a Nash-equilibrium.

Example in which Corollary 2 holds:

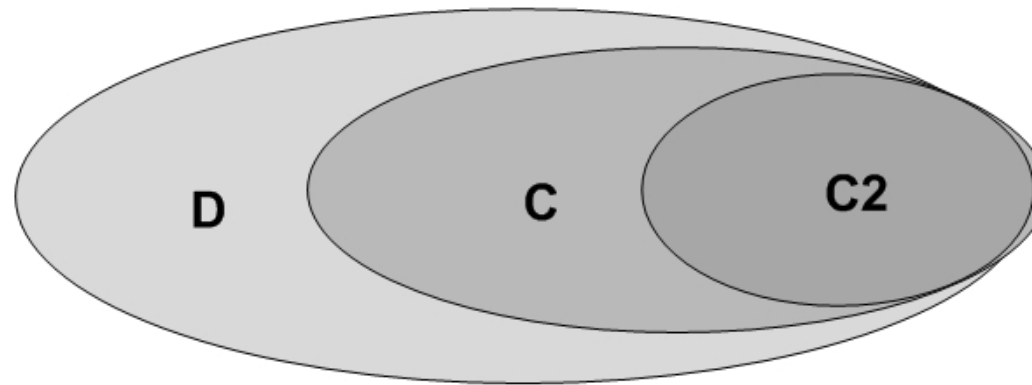


Network



Dependency graph

# Classification of Scenarios



**D:** Set of scenarios, in which every node playing AllD is a Nash equilibrium

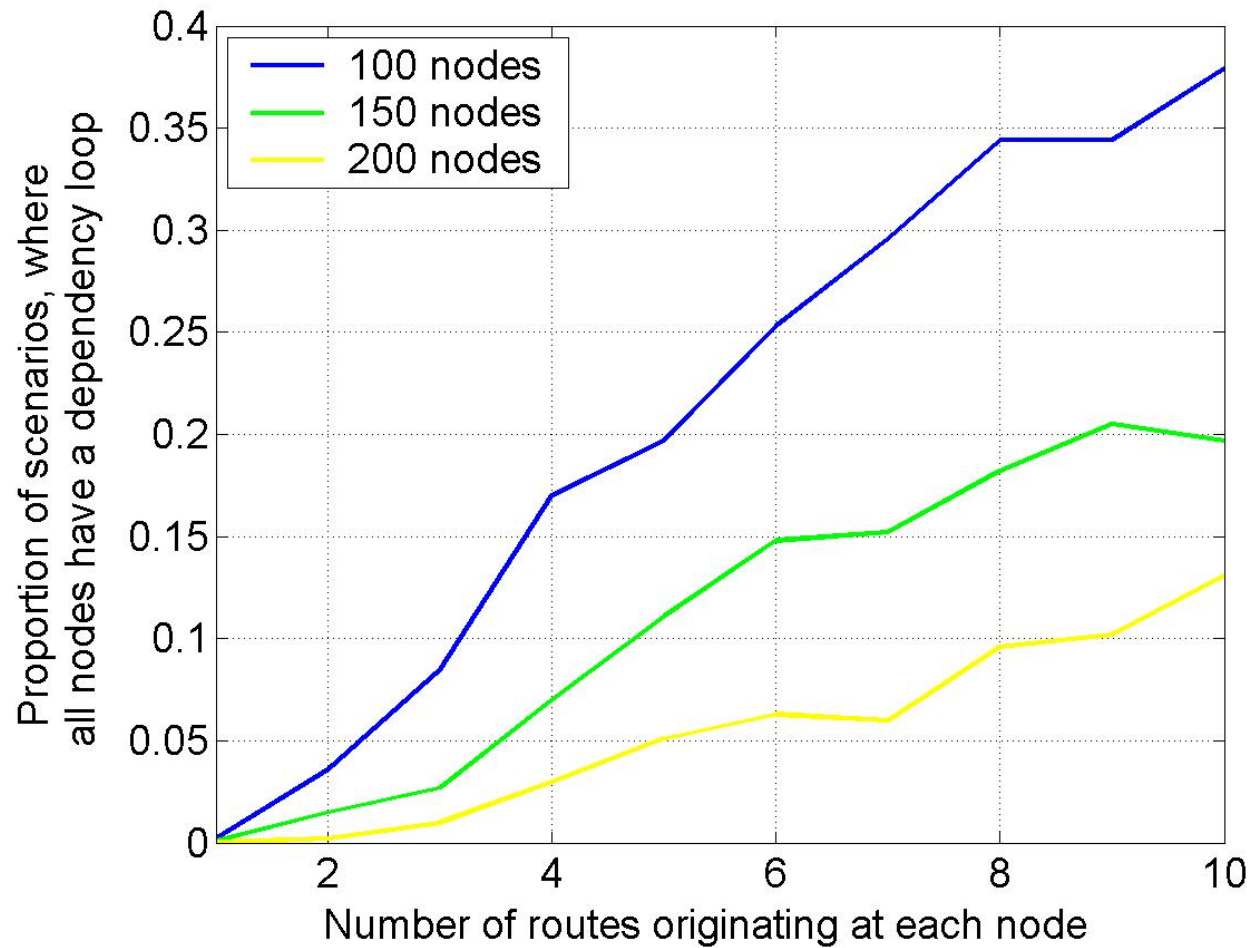
**C:** Set of scenarios, in which a Nash equilibrium based on cooperation is not excluded by Theorem 1

**C2:** Set of scenarios, in which cooperation is based on the conditions expressed in Corollary 2

# Simulation settings

Number of nodes	100, 150, 200
Distribution of the nodes	random uniform
Area type	torus
Area size	1500x1500m, 1850x1850m, 2150x2150m
Radio range	200 m
Number of routes originating at each node	1-10
Route selection	shortest path
Number of simulation runs	1000

# Simulation results



# Summary

## ➤ **Analytical results:**

- If everyone drops all packets, it is a Nash-equilibrium
- **In theory**, given some conditions, a cooperative Nash-equilibrium can exist ( i.e., each forwarder forwards all packets )

## ➤ **Simulation results:**

- **In practice**, the conditions for cooperative Nash-equilibria are very restrictive : the likelihood that the conditions for cooperation hold for every node is extremely small

## ➤ **Consequences:**

- Cooperation cannot be taken for granted
- Mechanisms that stimulate cooperation are necessary
  - incentives based on virtual currency
  - reputation systems